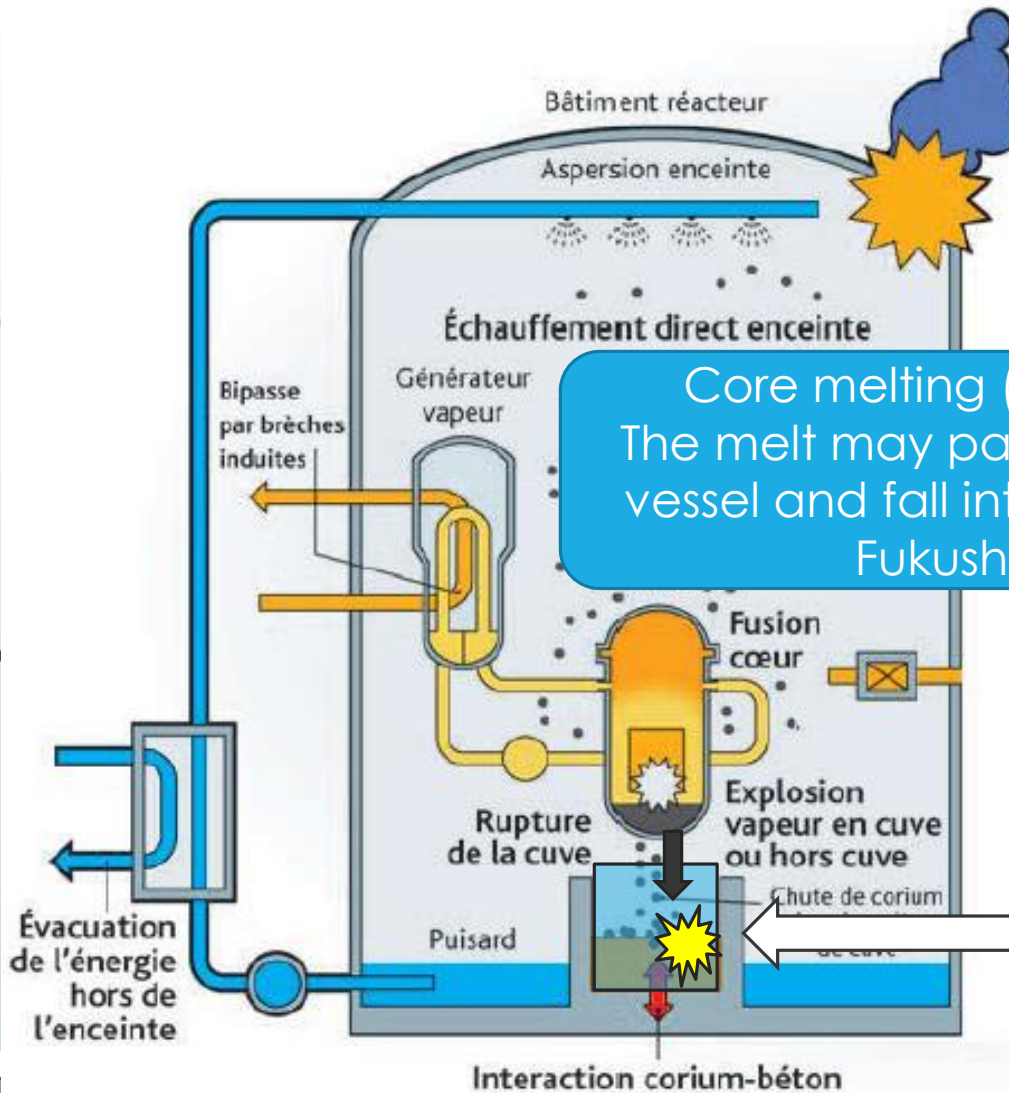


# Experimental Study of Liquid-Liquid Fragmentation

Bowen Ji, Gagan Kewalramani, Nicolas Rimbert, Yvan Dossmann,  
Michel Gradeck

LEMTA CNRS Université de Lorraine, 2 Avenue de la Forêt de Haye,  
54518, Vandoeuvre-les-Nancy, France

# The Project



Source: Livre d'accidents graves IRSN

Core melting ( $\Rightarrow$  corium  $\sim 3000$  K)  
The melt may pass through the reactor vessel and fall into the reactor pit (e.g. Fukushima Daiichi)

Steam explosion risk in mitigation strategies with water in the reactor pit (In-Vessel Retention)

# Simplifying Assumptions

- Gas-liquid atomization has been studied a lot!
- Liquid-liquid atomization is easier!
- No vapour!
- The goal: understand the mechanism!

# Experimental Facility

- Electromagnetically controlled injector:
- Pneumatic pressure control
- Cargille fluid (transparent) is injected in water tank of 50x50x40 cm<sup>3</sup>

	$\rho$ (kg/m <sup>3</sup> )	$\mu$ (Pa-s)
Water	998.2	1.05
Cargille	1896.52	26.02

- Surface tension  $\sigma = 0.0265\text{N/m}$
- Jets with nozzle diameter 1,2,3 and 4 mm with various injection pressure are produced

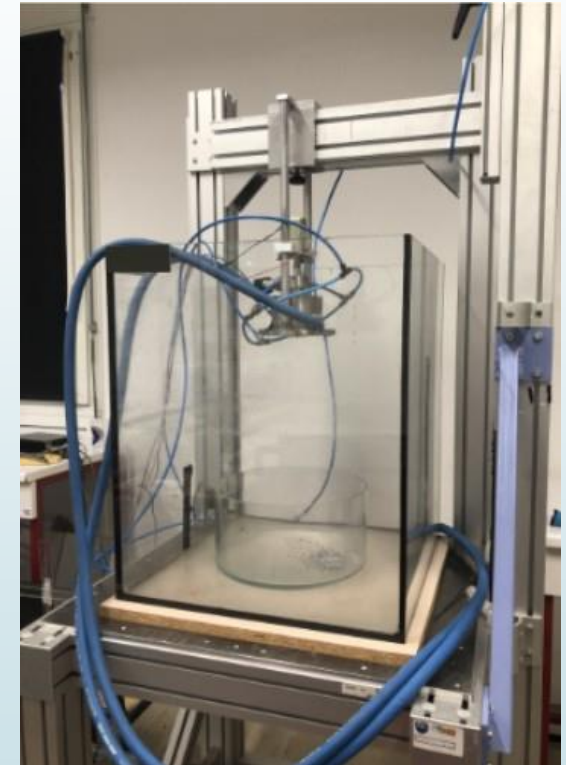
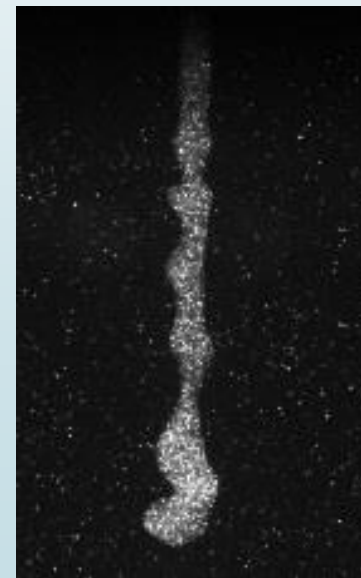
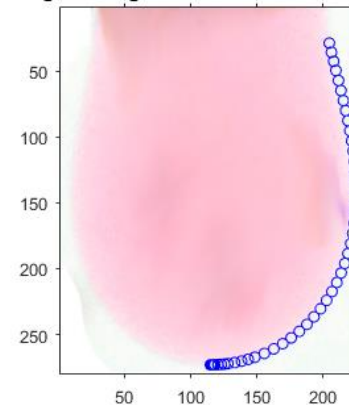


Figure: Experimental setup 'JaLad'

# Cargille Fluid

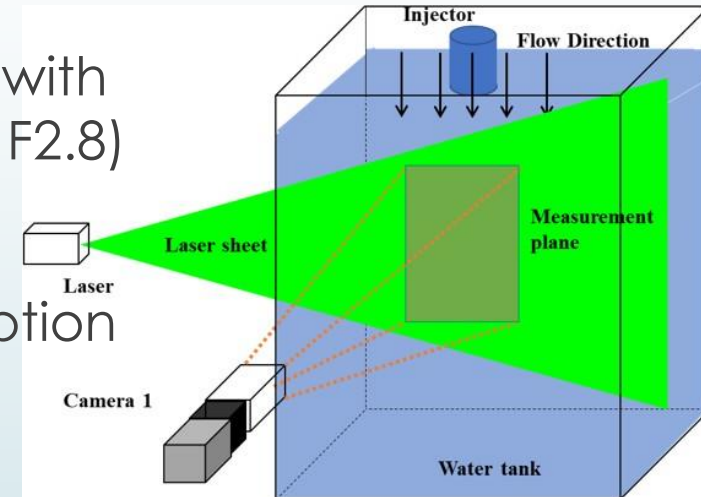
- Density
  - $\rho = 1896.52 \text{ kg/m}^3$
- Viscosity
  - $\mu = 26.02 \text{ mPa}\cdot\text{s}$
- Optical index
  - $n = 1.3330$  (id. eau)
- Surface tension
  - $\sigma = 0.0265 \text{ N/m}$
- Pyrrométhene 597
  - Fluorescent Dye

Original image + Contour + Fitted contour



# Cargille Fluid/Laser Sheet

- Laser sheet 532nm
- Camera records images with 9000 fps with lens of 150mm focus length (aperture F2.8)
- Images with pixel size of 99.5  $\mu\text{m}$
- Pyromethene 597-8C9 dye with absorption coefficient
- $a = 5.25 \cdot 10^{-4} L / (\text{mol} \cdot \text{cm})$  at 524nm



**Table 1** Velocity (in  $m/sec$ ), Diameter, Reynolds number ( $Re$ ) and Weber number ( $We$ ) for various jets.

Exp:	$U_0$	$Re$	$We$	Exp:	$U_0$	$Re$	$We$	Exp:	$U_0$	$Re$	$We$
D2V1	1.92	295	279	D2V2	2.96	455	663	D2V3	5.46	838	2248
D3V1	1.62	375	300	D3V2	3.13	764	1245	D3V3	5.96	1375	4027
D4V1	1.72	530	449	D4V2	3.05	938	1408	D4V3	5.90	1813	5256

# Non Dimensional Numbers

- Weber number

$$We_c = \frac{\rho_C U_\infty^2 2R_0}{\gamma}$$

- Ohnesorge number (or viscosity group)

$$Oh = \frac{\mu_L}{\sqrt{2R_0 \rho_L \gamma}}$$

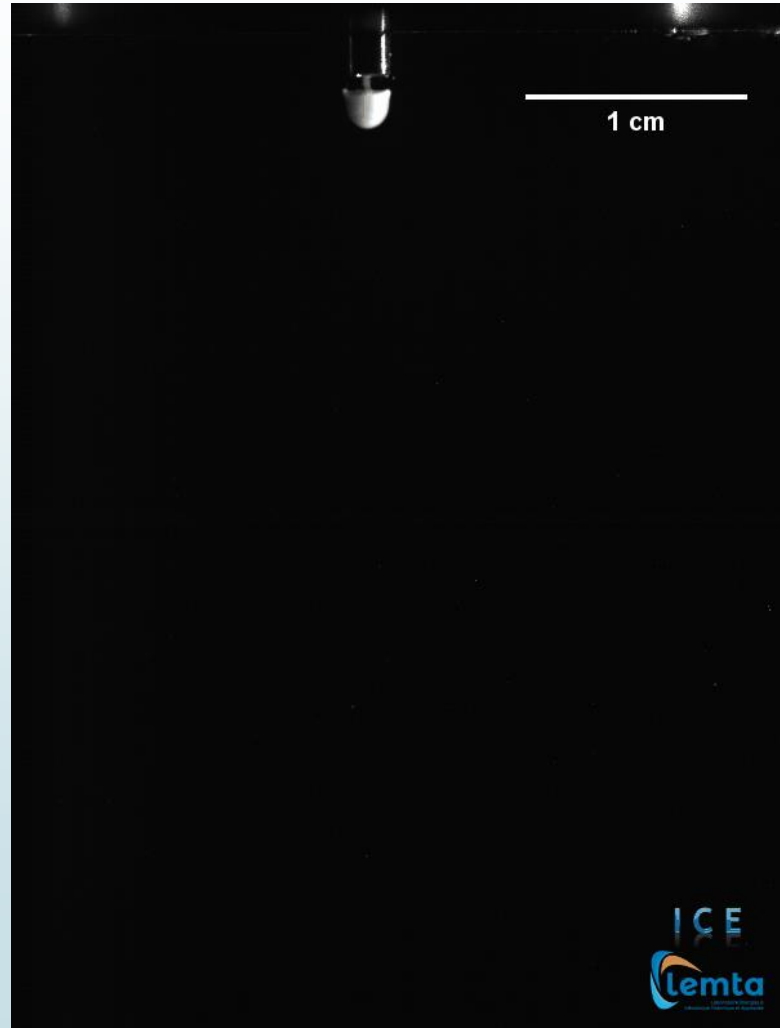
- Density ratio

$$\rho_R = \frac{\rho_L}{\rho_C}$$

- Viscosity Ratio

$$\mu_R = \frac{\mu_L}{\mu_C}$$

# Experimental Results





9

# 1 Lagrangian Analysis

# Tracks

Tracks is a commercial software

Filtering and Calibration

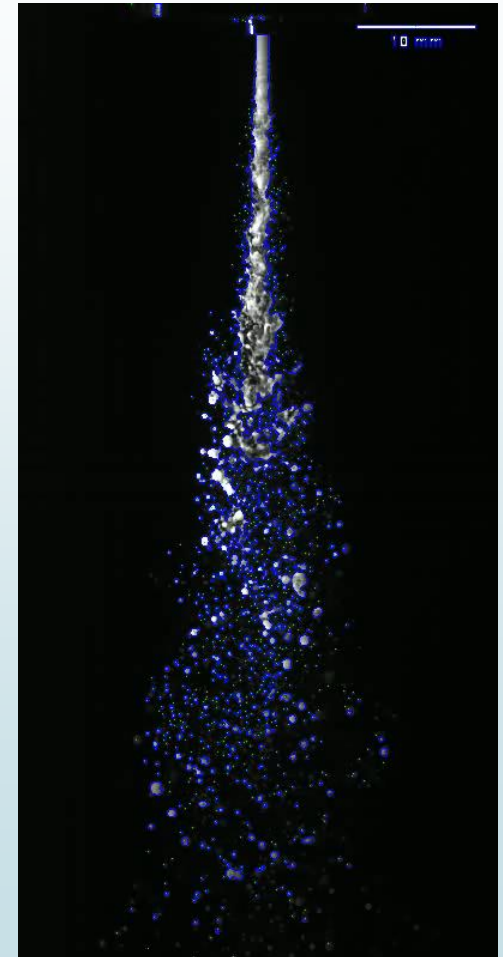


Detection



Tracking

- To reduce noise in images
  - background subtraction
  - Multiscale threshold method
  - in-homogeneous lighting and absorption effects.
- Droplet identification
  - clouds contour detection method

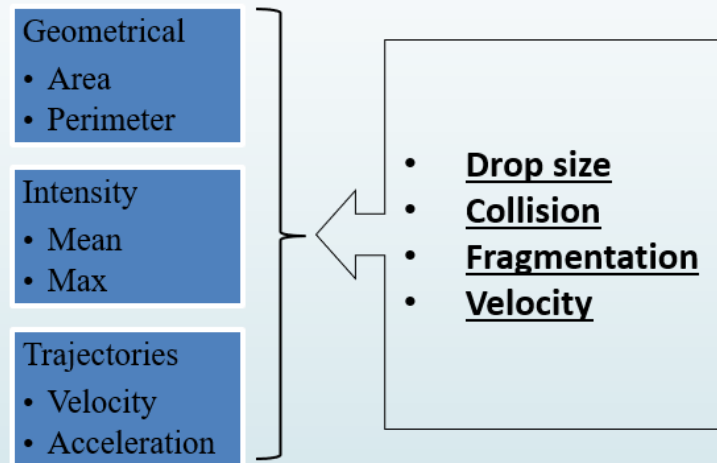


# Tracks

Drops are tracked with a predictive tracking algorithm using **Kalman filtering method**

For each ID, detection we may have various information.

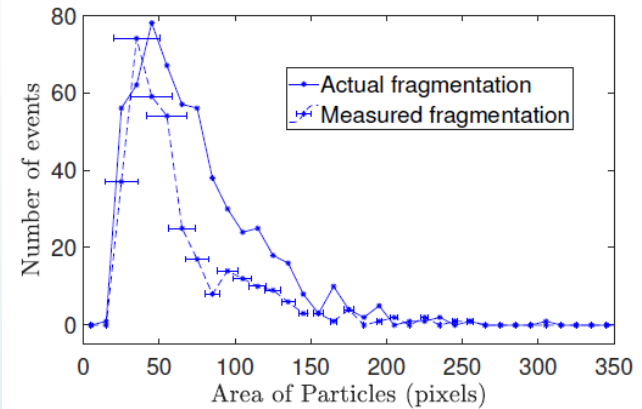
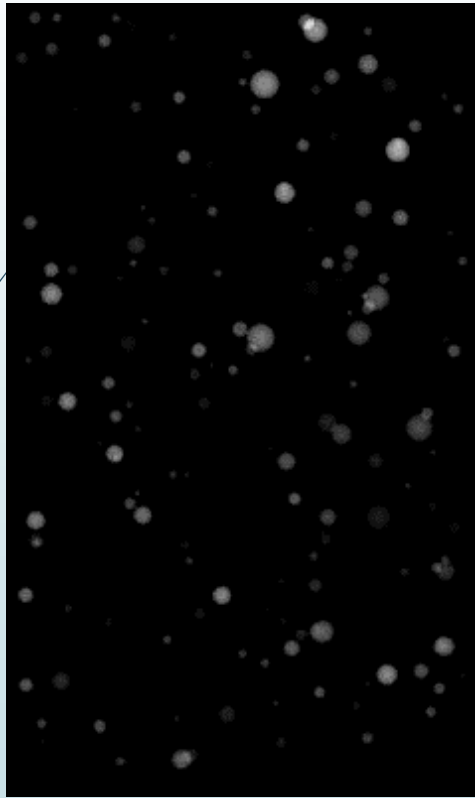
This information for ID is processed to identify events.



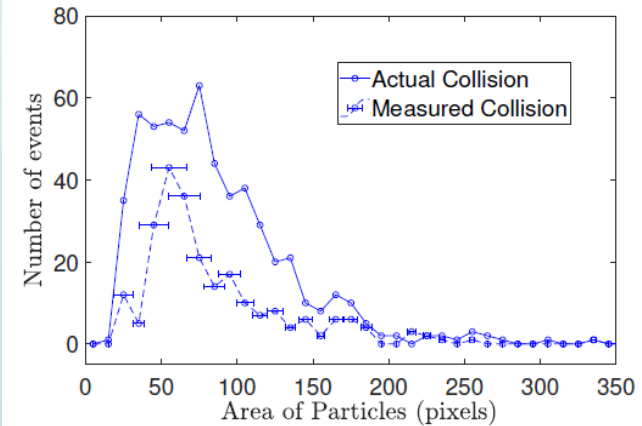
- For identifying collision and fragmentation constraints on

- Change in Area  $\frac{dA}{A}$
- Velocity Jump  $\frac{dV_{mag}}{V_{mag}}$
- Compactness  $C = \frac{4\pi \text{Area}}{\text{Perimeter}^2}$

# Synthetic Data for Validation



(a) Fragmentation events



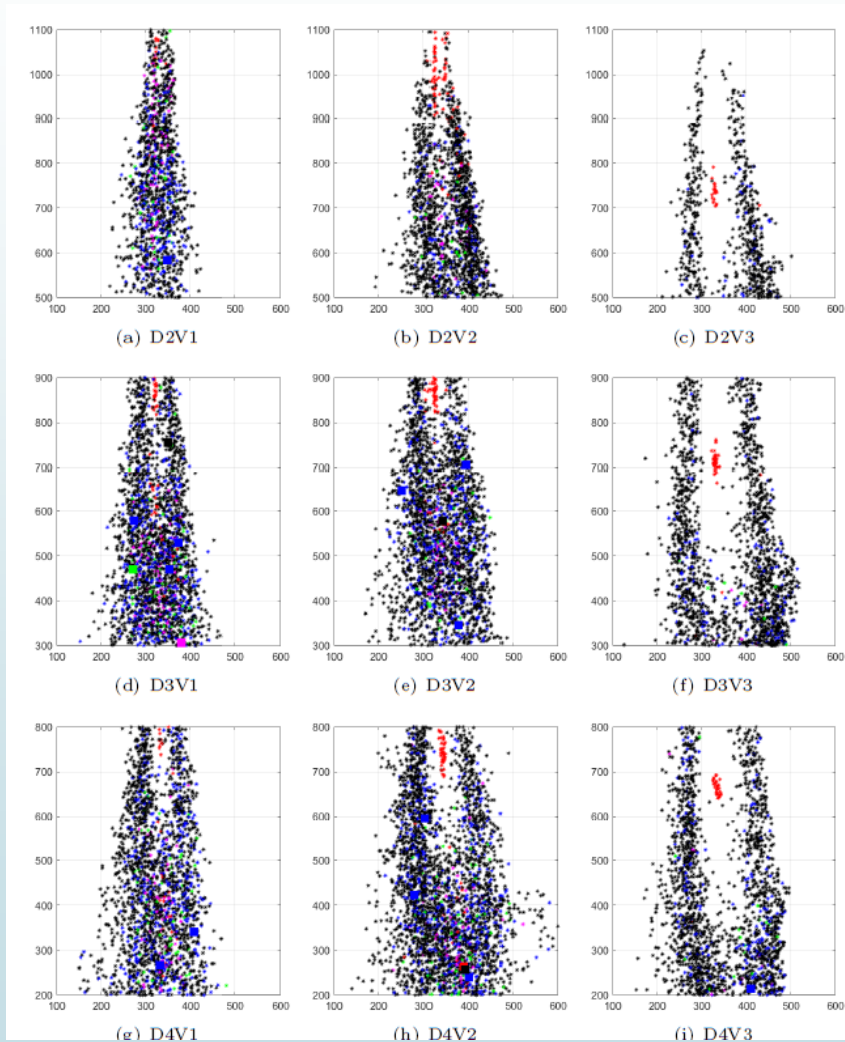
(b) Collision events

# Fragmentation Results

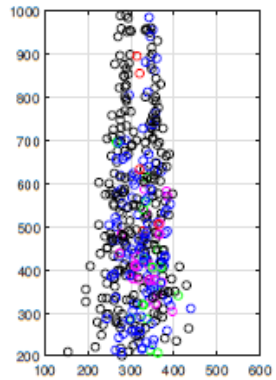
Primary and Secondary fragmentation results:

- Square Symbol for secondary fragmentation
- Star for Primary Fragmentation
  - Blue for size 20- 100 pix.
  - Black for size 100- 500 pix
  - Green for size 500- 1000 pix
  - Magenta for size 1000- 5000 pix
  - Red for size 5000 pix and above

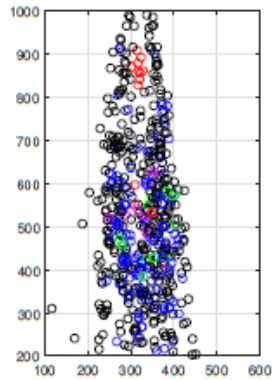
Horizontal axis represents pixels in radial direction and vertical axis represents pixels in axial direction



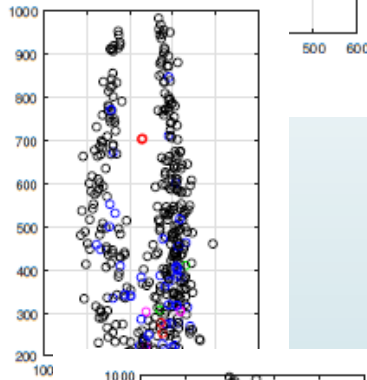
# Collision results



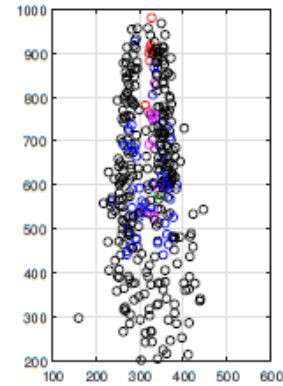
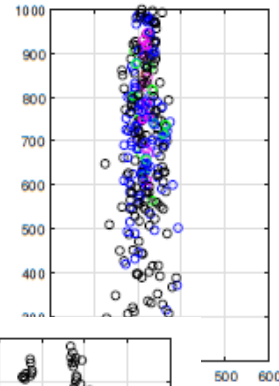
(d) D3V1



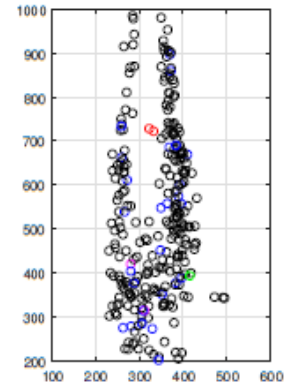
(e) D3V2



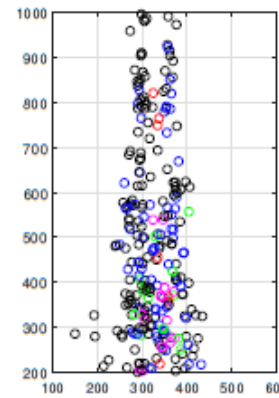
(g) D4V1



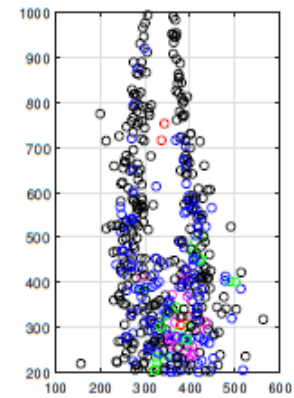
(b) D2V2



(c) D2V3



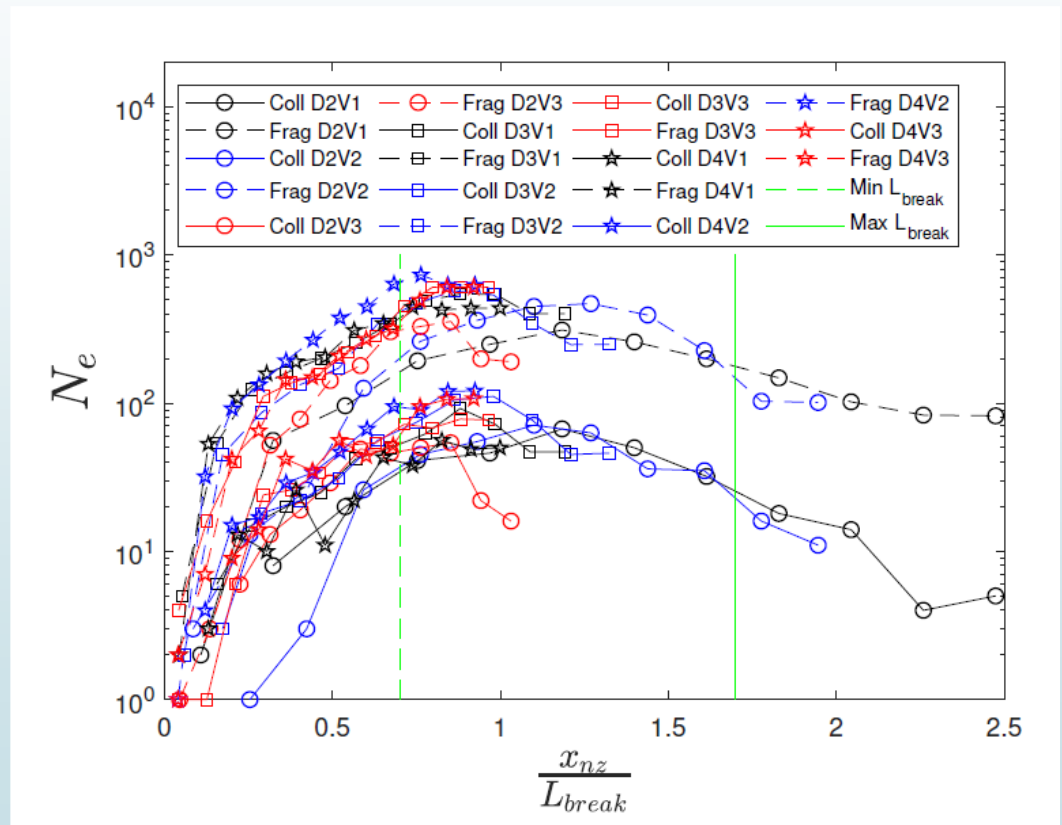
(h) D4V2



(i) D4V3

# Fragmentation vs. Collision

- Fragmentation are ten time more frequent than collision
- Submitted to experiments in Fluids...



16

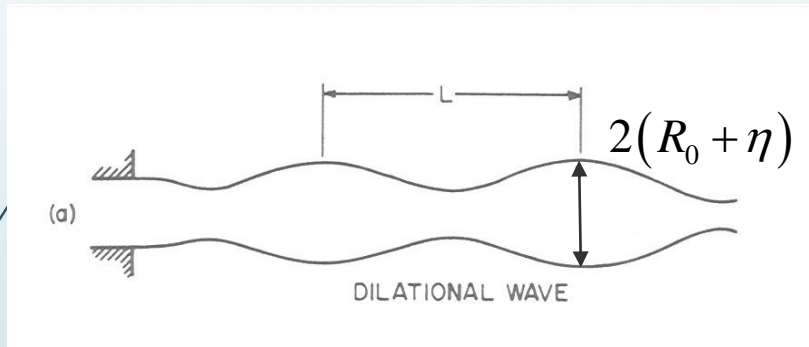
# 2 Eulerian Analysis and Instability Identification



# List of Instabilities

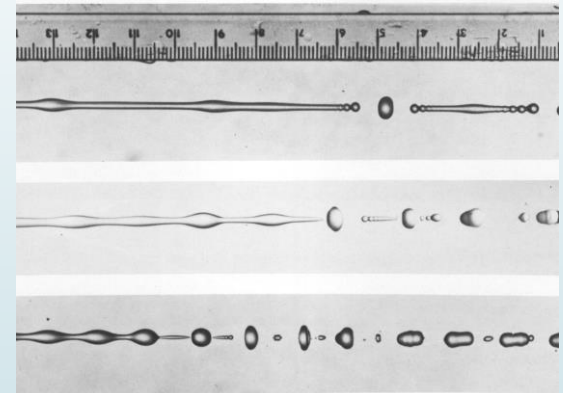
► Rayleigh-Plateau (1873)

$$kR_0 = 0.697$$



$$\eta = \eta_0 e^{(\sigma t + ikx)}$$

Lefebvre (1989)



Van Dyke (1982)

# List of Instabilities

- Planar Kelvin-Helmholtz (1871)

$$\frac{R_0}{\lambda_{KH, \max}} = \frac{1}{1 + \rho_R^{-1}} \frac{We}{12\pi}$$

- Weber (1931)

$$\sigma^2 + \sigma \frac{3\mu_L k^2}{\rho_L R_0^2} = \frac{\gamma}{2\rho_L R_0^3} (1 - k^2) k^2 + \frac{\rho_C}{\rho_L} \frac{U}{2R_0^2} k^3 \frac{K_0(k)}{K_1(k)}$$

- Reitz (1987)

$$\frac{\lambda}{R_0} = 9.02 \frac{(1 + 0.45 Oh^{0.5})(1 + 0.4T^{0.7})}{(1 + 0.87 We_C^{1.67})^{0.6}} \quad T = Oh \sqrt{We_C}$$

- Entov-Yarin (1984)

$$k_{EY, \max} = \left( \frac{8}{9} \frac{\rho_L R_0^2}{\mu_L^2} \left( \rho_C U_0^2 - \frac{\gamma}{R_0} \right) \right)^{1/6}$$

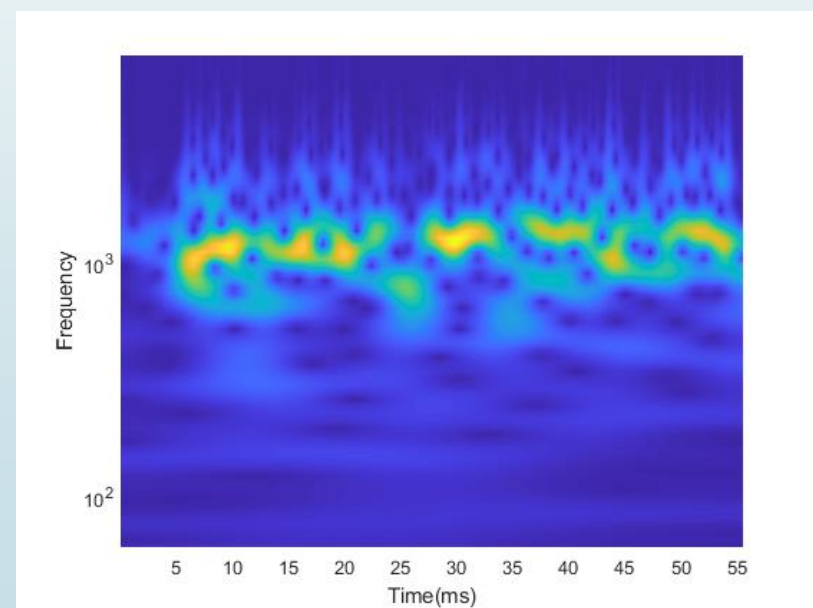
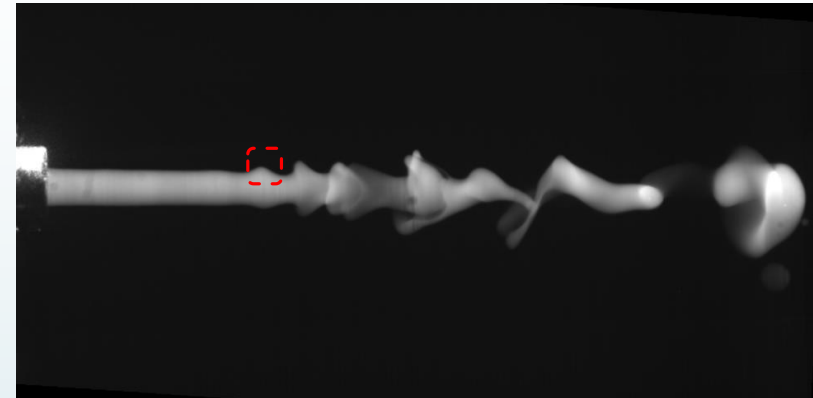
# Eulerian Analysis



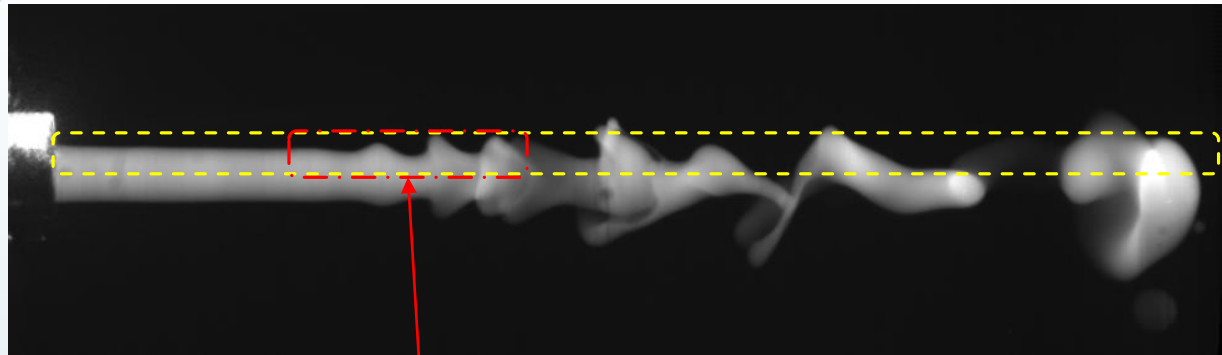
- Cargille fluid
  - $D_j = 1 \text{ mm}$
  - $U = 1.91 \text{ m/s}$
- Focus on the edge of the cross section of the jet
  - Spatial resolution:  $22.1 \text{ } \mu\text{m/pixel}$
  - Frame rate: 14000fps

# Analysis on Temporal frequency

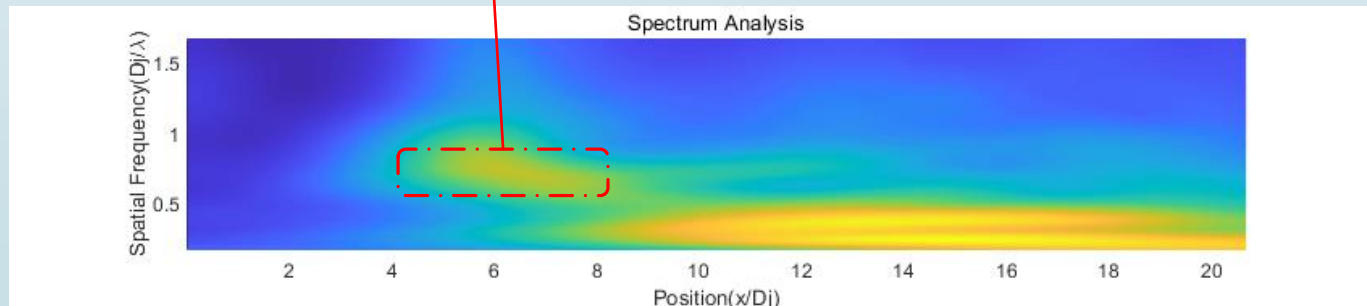
- ▶ A sample region of  $10 \times 10$  pixels is selected
- ▶ A Wavelet analysis is done for 1000 frames
- ▶ The result shows a fairly stable temporal frequency



# Analysis on Spatial frequency

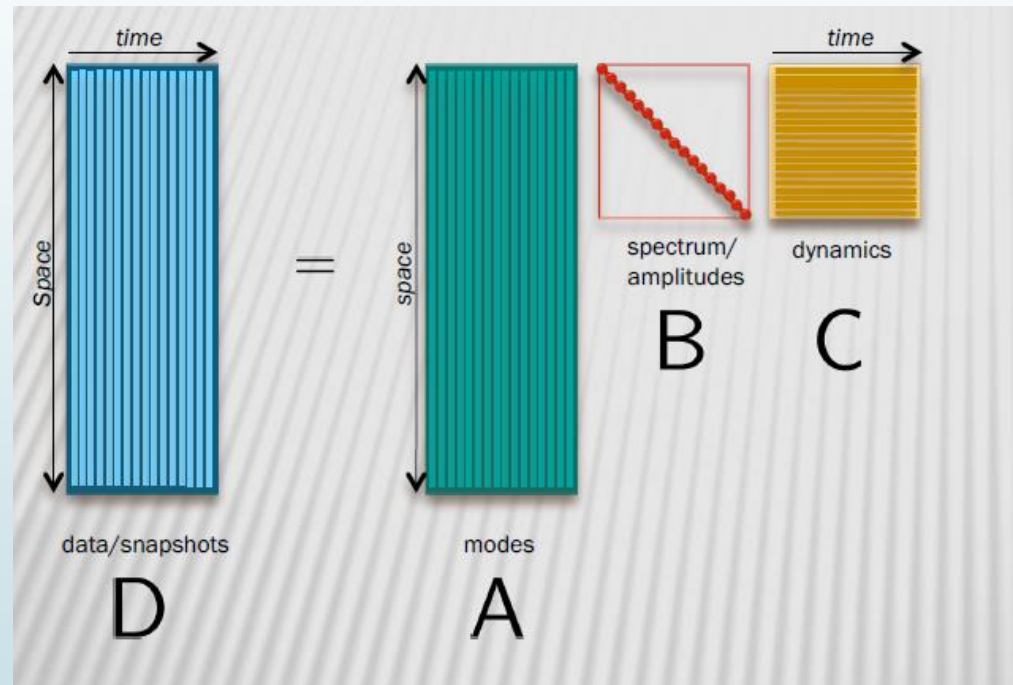


- A sample region of 20\*900 pixels is selected
- A Wavelet analysis is done on spatial frequency for 300 frames



# Dynamic Mode Decomposition

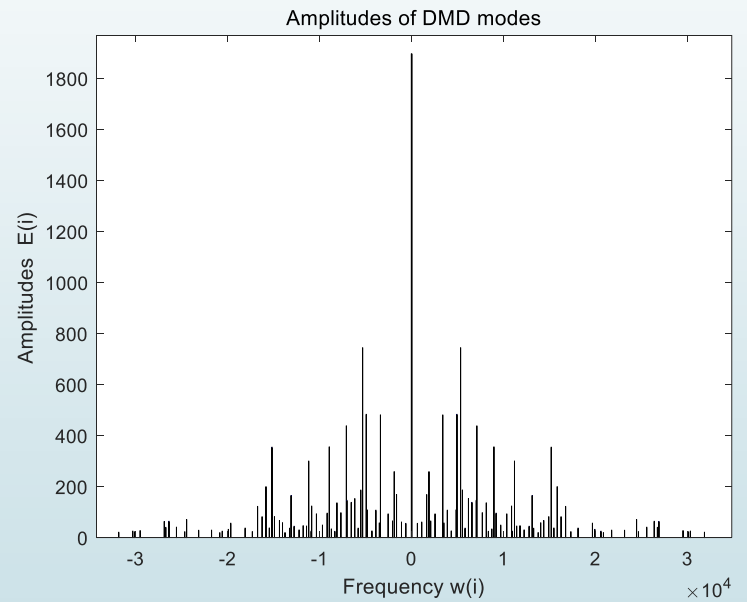
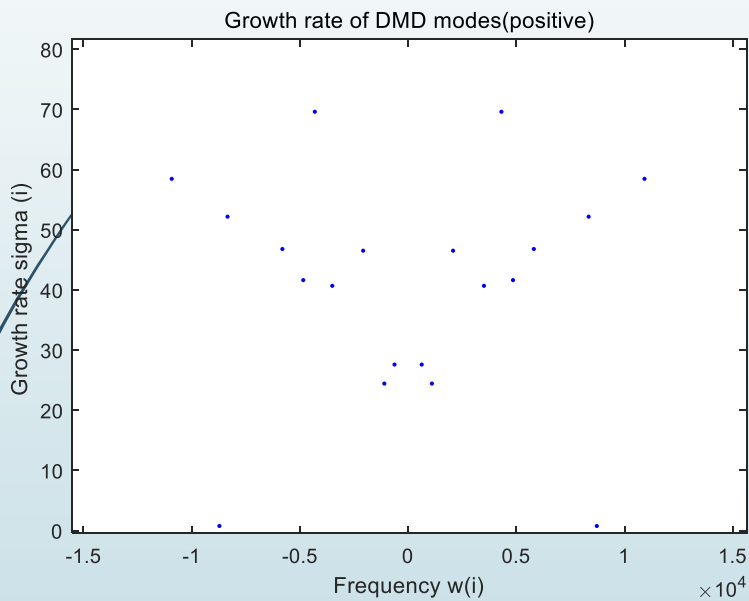
- ▶ Data Driven Method
  - ▶ Similar to POD (Proper Orthogonal Decomposition)
- ▶  $D = A B C$



Source: P. Schmidt

# DMD Analysis (1)

► Results of DMD analysis



# DMD Analysis (2)

- Modes with positive growth rates are extracted:

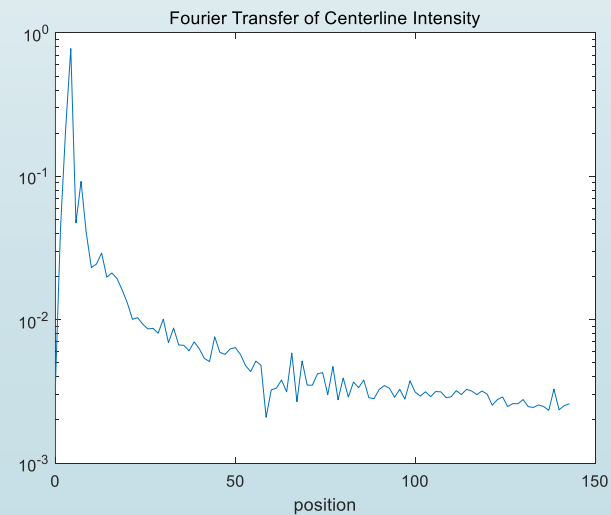
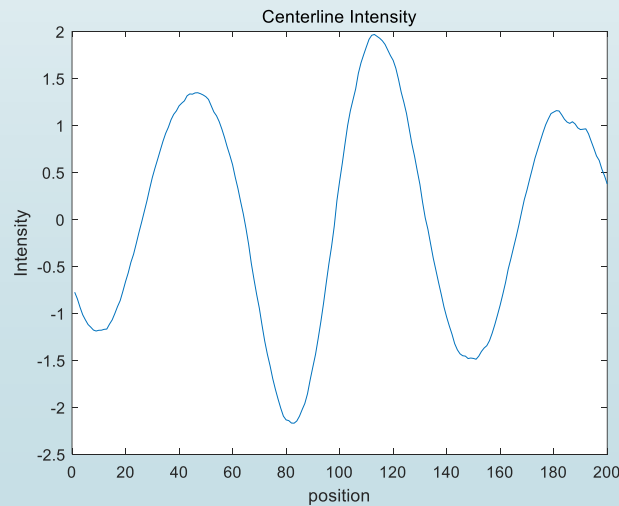
Mode	Growth Rate (s <sup>-1</sup> )	Amplitude	Frequency (Hz)
41	41.6	109	4846
61	46.5	65	2076
67	24.4	61	1099
71	40.7	57	3505
75	27.6	55	629
93	46.8	37	5809
99	0.8	34	8718
113	69.6	26	4311
117	58.5	25	10921
121	52.2	24	8341



# DMD Analysis (3)

- Intensity map of different modes are extracted
- A Fourier transform is done for the centerline
- The non dimensional spatial wavenumber and wavelength can be found

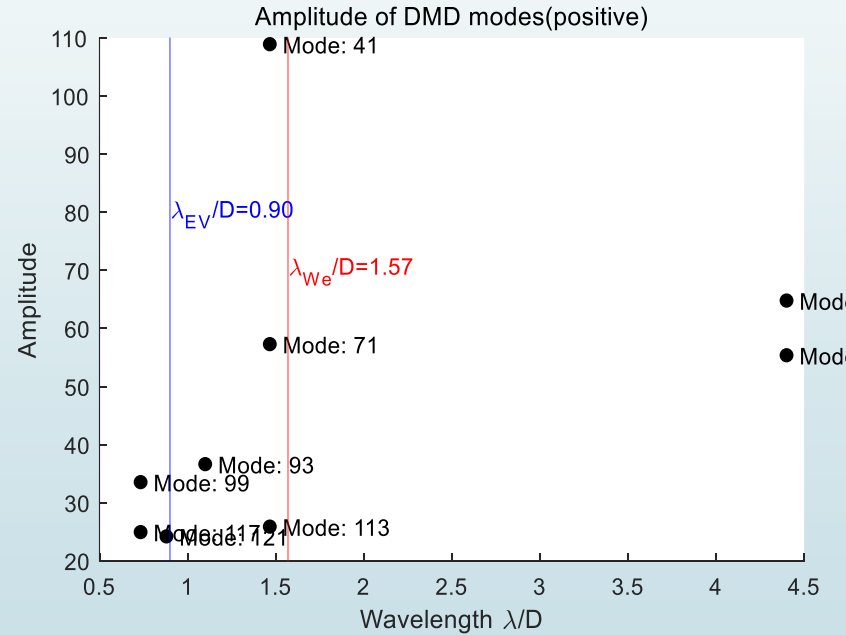
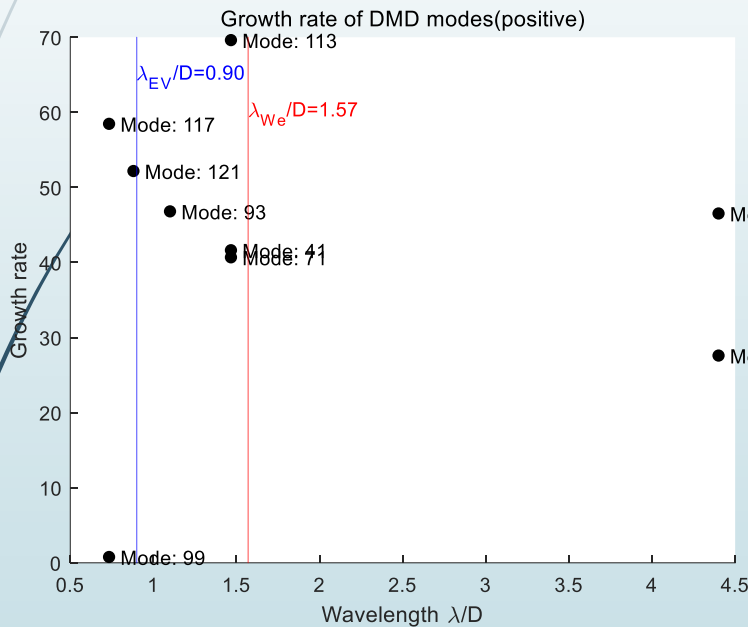
Mode: 41 growth rate: 41.6 amplitude: 109 frequency: 21



# DMD Analysis (4)

- Comparing instability with the result from DMD

D (mm)	P (bar)	U (m/s)	Re <sub>L</sub>	We <sub>C</sub>	$\lambda_T/D$	$\lambda_{We}/D$	$\lambda_{EY}/D$	$\lambda_{KH}/D$	$\lambda_{SS}/D$	$\lambda_{LK}/D$	$\lambda_R/D$
1	1	1.69	128	108	0.056	1.571	0.900	0.132	0.156	0.142	0.154



- The Weber instability model and Entov-Yarin instability model fits best with this result

# Conclusion

- Fragmentation dominates over collision
- Instability mechanisms are the root
  - Weber Instability and Entov-Yarin Bending Instability
  - Other atomizer, other instability

Thanks for your attention!